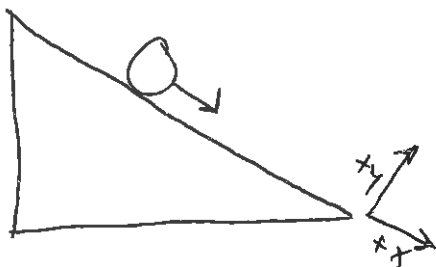


# Worksheet #2 Solutions

1 a.



Known:

$$t = 5 \text{ seconds}$$

$$\Delta x = x - x_0 = 50 \text{ meters}$$

$$v_0 = 0 \text{ m/s}$$

Unknown:

$a$

Ideally, we want to use an equation that has only one unknown variable. Luckily, we have one:

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

Solving for  $a$ ,

$$x - x_0 = \Delta x = v_0 t + \frac{1}{2} a t^2$$

$$\frac{1}{2} a t^2 = \Delta x - v_0 t$$

$$a = \frac{2(\Delta x - v_0 t)}{t^2} = \frac{2(50 - (0)(5))}{25} = \boxed{4 \text{ m/s}^2}$$

b. Now we know  $t$ ,  $v_0$ , and  $a$ , but not  $\Delta x$ . We can use the same equation, because we will still have only 1 unknown variable:

$$v_0 = 2.0 \text{ m/s}$$

$$a = 4 \text{ m/s}^2$$

$$\Delta x = v_0 t + \frac{1}{2} a t^2 = (2)(5) + \frac{1}{2}(4)(25) = \boxed{60 \text{ meters}}$$

c. We can do the same thing as part b, but now  $v = -2.0 \text{ m/s}$  because it is now uphill, which we have defined as the negative  $x$ -direction:

$$v_0 = -2.0 \text{ m/s} \quad \Delta x = (-2)(5) + \frac{1}{2}(4)(25) = \boxed{40 \text{ meters}}$$



Known:

$$v_0 = 20 \text{ m/s}$$

$$d = 50 \text{ m}$$

$$a = -3.8 \text{ m/s}^2$$

$$v_f = 0 \text{ m/s}$$

Unknown:

$$\Delta x, t$$

First, we will determine how long the car takes to stop. Next, we will use this to determine how far the car travels before stopping.

We need an equation for  $t$  that does not depend on  $\Delta x$ . Therefore,

we can use  $a = \frac{v_f - v_0}{t} \Rightarrow t = \frac{v_f - v_0}{a}$ .

Now, we plug this into our equation for  $\Delta x$ :

$$\begin{aligned} \Delta x &= v_0 t + \frac{1}{2} a t^2 \\ &= \frac{v_0 (v_f + v_0)}{a} + \frac{1}{2} \frac{a (v_f - v_0)^2}{a^2} \\ \Delta x &= \frac{20(-20)}{-3.8} + \frac{1}{2} \frac{(-3.8)(-20)^2}{(-3.8)^2} = 52.6 \text{ meters} \end{aligned}$$

So the car will not be able to stop before entering the intersection.

2 b.



Known:

$$v_0 = 20 \text{ m/s}$$

$$L = 3.5 \text{ m}$$

$$d = 50 \text{ m} + 20 \text{ m} = 70 \text{ m}$$

$$t = 3 \text{ s}$$

$$a = 2.3 \text{ m/s}^2$$

We must determine how far the car travels in 3 seconds and compare that to the distance needed to clear the intersection.

To do this, we can use

$$\Delta x = v_0 t + \frac{1}{2} a t^2 = (20)(3) + \frac{1}{2}(2.3)(3)^2$$

$$\Delta x = 70.35 \text{ m}$$

At first, it seems as if the car has made it. However, the entire car must make it through. The back of the car must travel  $d + L = 73.5$  meters to clear the intersection, so the car does not make it here either.