

Worksheet #3 Solution

Given $x = 3.0 \text{ m} + 4.0 \text{ m/s } t$; $y = 10 \text{ m/s } t - 4.9 \text{ m/s}^2 t^2$
 $(x = 3 + 4t)$ $(y = 10t - 4.9t^2)$

a. $v_x = \frac{dx}{dt} = \frac{d}{dt}(3 + 4t) = \boxed{4 \text{ m/s}}$

$v_y = \frac{dy}{dt} = \frac{d}{dt}(10t - 4.9t^2) = \boxed{(10 - 9.8t) \text{ m/s}}$

b. $a_x = \frac{dv_x}{dt} = \frac{d}{dt}(4) = \boxed{0 \text{ m/s}^2}$

$a_y = \frac{dv_y}{dt} = \frac{d}{dt}(10 - 9.8t) = \boxed{-9.8 \text{ m/s}^2}$

c. $v = \sqrt{v_x^2 + v_y^2} = \sqrt{(4)^2 + (10 - 9.8t)^2}$

$$= \sqrt{16 + 100 - 196t + 96.04t^2}$$

$$= \boxed{\sqrt{116 - 196t + 96.04t^2}}$$

d. $a = \sqrt{a_x^2 + a_y^2} = \sqrt{(0)^2 + (-9.8)^2} = \sqrt{(-9.8)^2} = \boxed{9.8 \text{ m/s}^2}$

e. $\frac{dv}{dt} = \frac{d}{dt}(\sqrt{116 - 196t + 96.04t^2}) = \frac{1}{2\sqrt{116 - 196t + 96.04t^2}} \cdot -196 + 192.08t$

$$= \frac{192.08t - 196}{2\sqrt{116 - 196t + 96.04t^2}} = \boxed{\frac{96.04t - 98}{\sqrt{116 - 196t + 96.04t^2} \text{ m/s}^2}}$$

g. (not f.)

$$a_{||} = \frac{\vec{a} \cdot \vec{v}}{v} = \frac{a_x v_x + a_y v_y}{v}$$

$$= \frac{(0)(4) + (-9.8)(10 - 9.8t)}{\sqrt{116 - 196t + 96.04t^2}}$$

$$= \boxed{\frac{96.04t - 98}{\sqrt{116 - 196t + 96.04t^2}} \text{ m/s}^2}$$

h. $\frac{dv}{dt}$ and $a_{||}$ should be the same, and they are.

$\frac{dv}{dt}$ and a should not necessarily be the same, as $\frac{dv}{dt} = \frac{d|\vec{v}|}{dt}$

while $a = |\vec{a}| = \left| \frac{d\vec{v}}{dt} \right|$ and $\frac{d|\vec{v}|}{dt} \neq \left| \frac{d\vec{v}}{dt} \right|$.