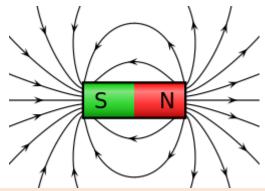
# Chapter 27: Magnetic Field and Magnetic Forces

- Magnetic field and magnets
- Magnetic flux and Gauss's law for magnetic field
- Magnetic force on moving charged objects
- Magnetic force on current-carrying wires
- Magnetic potential energy and torque
- Hall effect

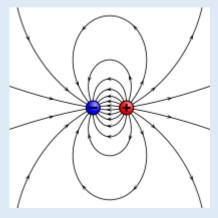
### Magnetic field and magnets

The magnet and the magnetic field produced by it

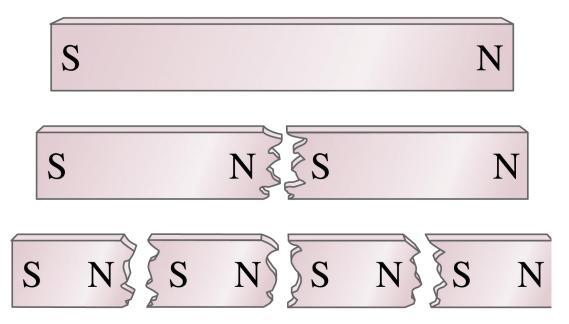


The magnetic field,  $\vec{B}$ , has a unit of Tesla  $(1T = 1N/A \cdot m)$ 

Very similar to the electric dipole and the electric field produced by it



### Breaking the magnets



Is that possible to break the magnet until you have single "N" or "S"?

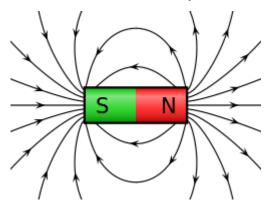
No! → There is no magnetic monopole exist!!

# Magnetic flux and Gauss's law for magnetic field

**Gauss's law for electric field**: for an closed surface, the electric flux passing through the surface only depends on the total enclosed charges in it.

$$\Phi_E = \oint_S \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\varepsilon_0}$$

**Gauss's law for magnetic field**: for an closed surface, the magnetic flux passing through the surface only depends on the total enclosed poles in it.



$$\Phi_B = \oint_{\mathcal{S}} \vec{B} \cdot d\vec{A} = 0$$
 (since any "N" is accompanied by an "S")

## Magnetic force on moving charged objects

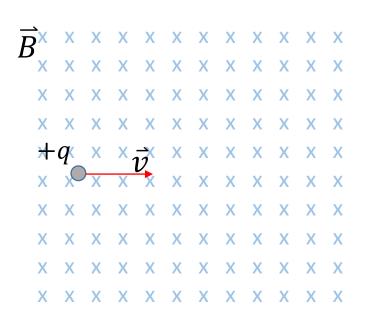
Charged particles "moving" in magnetic field will feel a magnetic force:

$$\vec{F}_m = q\vec{v} \times \vec{B}$$

Charged particles "moving" in magnetic field and electric field will feel both magnetic and electric forces:

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

When a particle with charge, +q, moving with a velocity toward right direction in a uniform magnetic field with the direction pointing into the screen, what direction of the magnetic force will this particle feels?

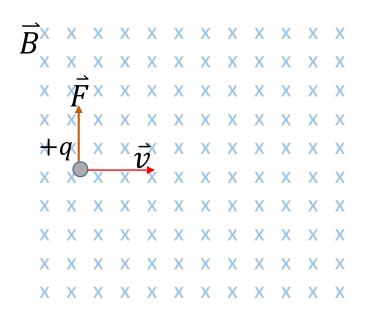


- A. Upward
- B. Downward
- C. Same as the velocity direction
- D. Opposite of the velocity direction
- E. Out of the screen
- F. Into the screen

#### Example:

A beam of proton ( $q = 1.6 \times 10^{-19}C$ ) moves at  $3.0 \times 10^{5}m/s$  through a uniform 2.0-T magnetic field directed along the positive z-axis. The velocity of each proton lies in the xz-plane and is directed at  $30^{\circ}$  to the +z-axis. Find the force on a proton.

When a particle with charge, +q, moving with a velocity toward right direction in a uniform magnetic field with the direction pointing into the screen, what type of the motion does this charged particle move?



- A. Circular motion with counterclockwise direction
- B. Circular motion with clockwise direction
- C. Parabolic motion toward upward
- D. Parabolic motion toward downward
- E. Straight motion with positive acceleration
- F. Straight motion with negative acceleration

#### Worksheet for R and $\omega$

#### 

What is the force feel by the current-carrying wire?

Each electron has a force:

$$d\vec{F}_m = -e\vec{v}_d \times \vec{B}$$

The total force for electrons in the length L

$$\vec{F}_m = -e\vec{v}_d \times \vec{B} \cdot N$$

(N: the total number of electrons in the length L)

 $\times$   $\times$   $\times$   $\times$   $\times$   $\times$   $\times$   $\times$   $\times$ 

The total number of the electrons in the length L

$$N = n \cdot V = n \cdot A \cdot L$$

(V: Volume; A: Cross-section area; L: Length)

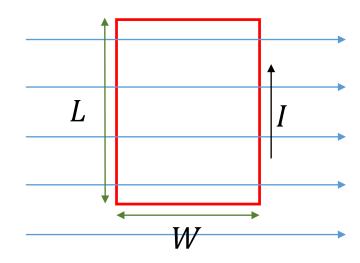
The total force feels by the wire

$$\vec{F}_m = I\vec{l} \times \vec{B}$$

What is the total force of this current-carrying loop in an uniform magnetic field?

 $\overrightarrow{B}$ 

And what is the total torque of this current-carrying loop in an uniform magnetic field?



$$\vec{F} = 0$$

$$\vec{\tau} = IAB \ (up \ direction)$$

A: the loop area

$$\vec{\tau} = I\vec{A} \times \vec{B}$$

Define: Magnetic dipole moment

$$\vec{\mu} = I\vec{A}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

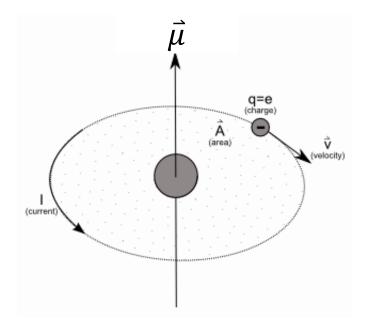
### Magnetic dipole moment

Define: Magnetic dipole moment

$$\vec{\mu} = I\vec{A}$$

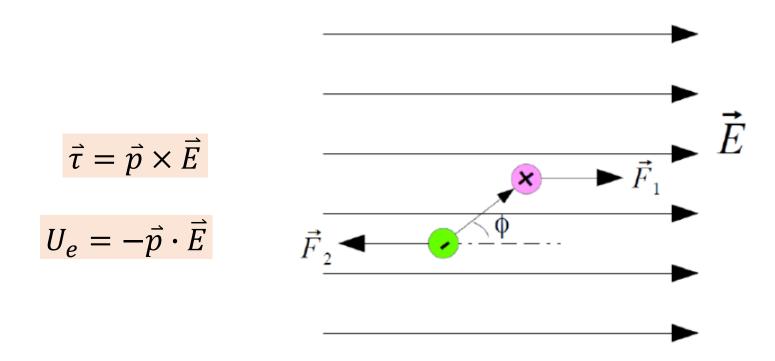
A loop of current is a magnetic dipole moment!!

#### Electrons in an atom



## Magnetic torque and potential energy of a magnetic dipole moment in magnetic field

Do you remember the electric torque and potential energy of a electric dipole moment in electric field?

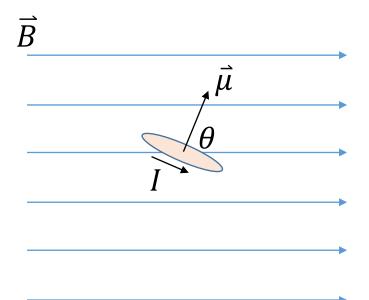


### Magnetic torque and potential energy of a magnetic dipole moment in magnetic field

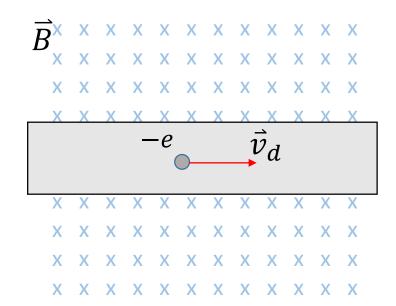
Do you remember the electric torque and potential energy of a electric dipole moment in electric field?

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

$$U_m = -\vec{\mu} \cdot \vec{B}$$



At this moment, how will this electron move? Assuming the size of the wire is smaller than the radius of the circular motion of the electron.



- A. Move upward and stay on top edge of the wire
- B. Move upward then straight to the right after hitting the top edge of the wire
- C. Move downward and stay on bottom edge of the wire
- D. Move downward then straight to the right after hitting the bottom edge of the wire
- E. Move straight

#### Hall effect

- The accumulated charges on the top/bottom of the wire will build up an electric field to prevent further charge build up.
- The built-up electric field could be measured by the potential difference between the top and bottom edges of the wire.
- This could be used to measure the magnetic field strength and the polarity of the moving charges.

