

# Temperature and Heat

Temperature is empirically rooted, but can also be described on a fundamental, microscopic level.

Temperature scales:

Fahrenheit	Celsius	Kelvin	
212	100	373.15	H <sub>2</sub> O boils
32	0	273.15	H <sub>2</sub> O freeze
-459.67	-273.15	0	abs. 0

$$T_F = \frac{9}{5}T_C + 32^\circ$$

$$T_C = \frac{5}{9}(T_F - 32^\circ)$$

$$T_K = T_C + 273.15$$

Thermometers work by bringing some device into thermal contact with a body to be measured.

## Zerth Law of Thermo

If C is in thermal eq<sup>m</sup> with A & B, then A & B are in eq<sup>m</sup>

## Some ways to measure T

- volume expansion of a liquid in a tube
- change of pressure in a gas
- change in resistivity of a wire
- differential change in length of a bi-metallic strip

## Absolute temperature

Pressure is  $\propto$  to  $T(K)$  at constant volume

$$\frac{P_1}{P_2} = \frac{T_1}{T_2} \quad \text{lets compare pressures at } 0^\circ\text{C and } 40^\circ\text{C}$$

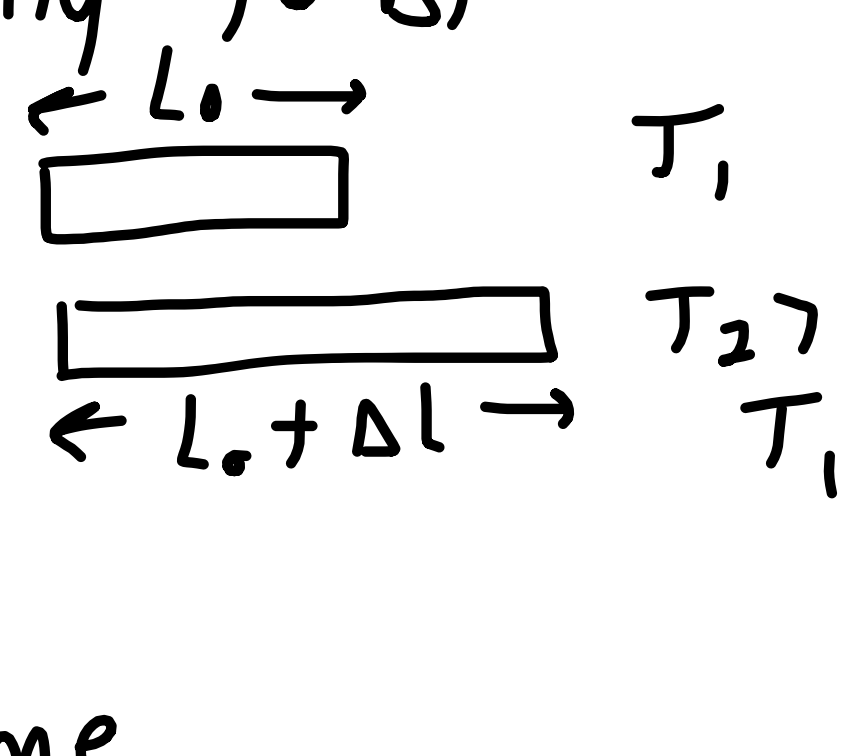
$$P_1 = 1 \text{ atm} \quad (273.15\text{K}) \quad (313.15\text{K})$$

$$P_2 = P_1 \cdot T_2 / T_1 = 1 \text{ atm} \cdot \frac{313\text{K}}{273\text{K}} = \boxed{1.15 \text{ atm}}$$

## Thermal Properties of matter

### Linear expansion

For moderate temp changes  $\Delta T$ , experiments show that materials expand proportionally to  $\Delta T$

$$\frac{\Delta L}{L_0} = \alpha \Delta T$$


Same idea for volume

$$\Delta V / V = \beta \Delta T \quad V_0 + \Delta V = V_0 + V_0 \beta \Delta T$$

Demo w/a bi-metallic strip

Brass  $\alpha = 2.0 \cdot 10^{-5} \text{ K}^{-1}$   
 Steel  $\alpha = 1.2 \cdot 10^{-5} \text{ K}^{-1}$  } Brass lengthens more  
 → curves "away" from Brass

### Problem

The Taipei 101 is 1671' tall. (at 15.5°C).


On a hot day, it is 0.471' taller. What is  $T_2$ ?

Building is made of steel

$$\Delta L = \alpha L_0 \Delta T \Rightarrow T_2 = T_1 + \Delta T = 15.5^\circ\text{C} + \Delta T$$

$$\Delta T = \frac{\Delta L}{\alpha L_0} = \frac{0.471 \text{ ft}}{1.2 \cdot 10^{-5} \text{ }^\circ\text{C}^{-1} (1671 \text{ ft})} = 23.5^\circ\text{C}$$

$$\rightarrow T_2 = 15.5^\circ\text{C} + 23.5^\circ\text{C} = 39.0^\circ\text{C}$$

S2.html  imagine cutting the donut and laying it flat

S3.html 
$$\frac{\Delta V}{V_0} = \frac{V_f - V_0}{V_0} = \frac{(V_0 + V_0 \beta \Delta T) - V_0}{V_0} = \beta \Delta T$$

cube: 
$$\frac{\Delta V}{V} = \frac{[(L_0 + L_0 \alpha \Delta T)(L_0 + L_0 \alpha \Delta T)(L_0 + L_0 \alpha \Delta T) - L_0^3]}{L_0^3}$$

$$= 1 + 3\alpha \Delta T + 3\alpha^2 \Delta T^2 + \alpha^3 \Delta T^3 - 1$$

$$\approx 3\alpha \Delta T \quad \text{since } \alpha \Delta T \ll 1$$

$$\rightarrow \beta \approx 3\alpha$$