

# Ch 4 solutions

(1)

19) There are two paths here. The first is longer but is based on the 1<sup>st</sup> Law.

$$\Delta U = Q - W \rightarrow Q = \Delta U + W = n C_V \Delta T + p \Delta V \quad (\text{since } p = \text{constant})$$

$$T_2 = T_1 p_2 V_2 / p_1 V_1 = 273.15 \frac{1.0}{1.0} \frac{3}{1} = 819.45 \text{ K} \Rightarrow \Delta T = 546.3 \text{ K}$$

$$V_1 = n R T_1 / p_1 = \frac{1 \cdot 8.3145 \cdot 273.15}{1.013 \cdot 10^5} = 0.02242 \text{ m}^3$$

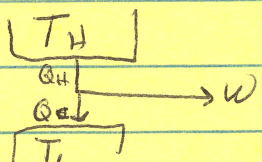
$$V_2 = 3V_1 = 0.06726 \text{ m}^3 \Rightarrow \Delta V = 0.04484 \text{ m}^3$$

$$\Rightarrow Q = 1 \cdot \frac{3}{2} R (546.3) + 1.013 \cdot 10^5 \cdot 0.04484 = \boxed{1.14 \cdot 10^4 \text{ J}}$$

$$\text{Shortcut: } Q = n C_p \Delta T = 1 \cdot \frac{5}{2} R 546.3 = \boxed{1.14 \cdot 10^4 \text{ J}}$$

$$20) W = \int p dU = n R T_1 \int \frac{dV}{V} = n R T_1 \ln \frac{V_2}{V_1} \quad \text{since } T = \text{constant}$$

$$= 1 \cdot 8.3145 \cdot \ln 2 = \boxed{1717 \text{ J}}$$

26) 

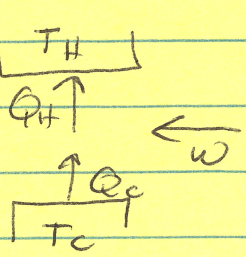
a)  $W = e Q_H = 0.3 \cdot 500 = \boxed{150 \text{ J}}$

b)  $e = 1 - \frac{Q_C}{Q_H} \Rightarrow Q_C = Q_H (1 - e) = \boxed{350 \text{ J}}$

28)  $Q_H / \text{hour} = 100,000 \text{ kg} \cdot 30 \cdot 10^6 \frac{\text{J}}{\text{kg}} = 3 \cdot 10^{12} \text{ J/hour}$

Work/hour =  $500 \cdot 10^6 \text{ W} \cdot 3600 \text{ s/hr} = 1.8 \cdot 10^{12} \text{ J/hour}$

}  $e = \frac{W}{Q_H} = \boxed{0.6}$

31) 

a)  $Q_H = 80 \text{ J} \quad k_R = 6.0 \quad \frac{1}{k_R} = \frac{Q_H - Q_C}{Q_C} = \frac{Q_H}{Q_C} - 1$

$\rightarrow Q_H / Q_C = \frac{1}{k} + 1 \rightarrow Q_C = Q_H / \frac{1}{k} + 1 = \boxed{68.6 \text{ J}}$

b)  $W = Q_C / k_R = \boxed{11.4 \text{ J}}$

32) a)  $Q_c = k_R W = \boxed{600 \text{ J}}$   
 b)  $Q_H = Q_c (k + 1) = \boxed{800 \text{ J}}$

33)  $k_p = \frac{T_c}{T_H - T_c} = \frac{200.15}{543.15 - 200.15} = \boxed{0.584}$

34)  $W = Q_c / k_R$  where  $Q_c = 1.0 \text{ J}$  and  $k_R = \frac{T_c}{T_H - T_c}$  assuming  $T_c = 0.15 \text{ K}$   
 a)  $\boxed{0.07 \text{ J}}$     b)  $\boxed{0.50 \text{ J}}$     c)  $\boxed{2.0 \text{ J}}$     d)  $\boxed{2000 \text{ J}}$

67)  $k_p = \frac{T_H}{T_H - T_c} = \frac{295.15}{22} = 13.416$

$Q_H = W \cdot k_p = 300 \text{ W} \cdot 3600 \text{ s} \cdot 13.416 = \boxed{1.45 \cdot 10^7 \text{ J}}$

81)  $e = 1 - T_c / T_H = 0.545$      $Q_H = 10^4 \text{ J}$   
 $e = W / Q_H \Rightarrow W = e Q_H = 5450 \text{ J per cycle}$   
 $\Rightarrow 5450 \text{ J/s} = \boxed{1090 \text{ Watts}}$