

## Exam 2 Review Session

#9 c)

$$\#10 \text{ b) } U = \frac{1}{2} C V^2 = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} Q V \Rightarrow U \text{ drops by factor of 4}$$

#11 a) 

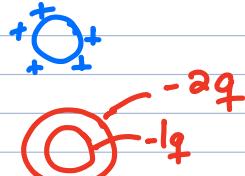
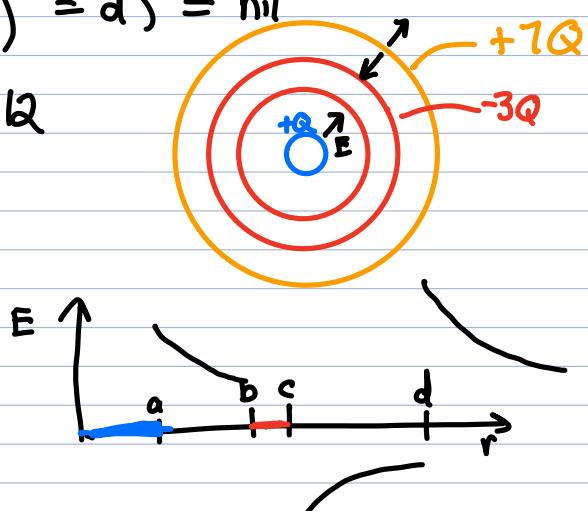
$$\text{b) } E_x = \frac{2kQ}{\text{dist} \sqrt{\text{dist}^2 + (\frac{a}{2})^2}} = \frac{2kQ}{\frac{a}{2} \sqrt{(\frac{a}{2})^2 + (\frac{a}{2})^2}} = \frac{4\sqrt{2} kQ}{a^2} (-j)$$

$$(\text{from the exam: } \frac{kQ}{x \sqrt{x^2 + l^2}})$$

$$E_y = \frac{4\sqrt{2} kQ}{a^2} (-j) \quad E_z = 0$$

c) = d) = nil

#12



$$\vec{E}(r < a) = 0$$

$$\vec{E}(a < r < b) = \frac{kQ}{r^2} \hat{r}$$

$$\vec{E}(b < r < c) = 0$$

$$\vec{E}(c < r < d) = -\frac{2kQ}{r^2} \hat{r}$$

$$\vec{E}(r > d) = +\frac{5kQ}{r^2} \hat{r}$$

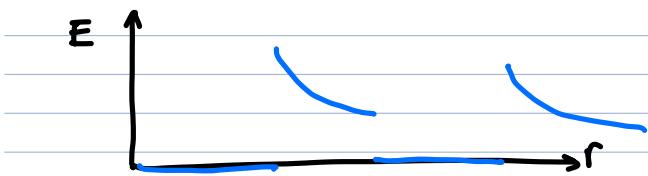
$$\underline{V(r > d)} \quad V_r - V_\infty = \int_r^\infty \vec{E} \cdot d\hat{r} = \int_r^\infty \frac{5kQ}{r^2} dr = -\frac{5kQ}{r} \Big|_r^\infty = 0 + \frac{5kQ}{r}$$

$$\Rightarrow V(r) = \frac{5kQ}{r} + V_\infty = \frac{5kQ}{r}$$

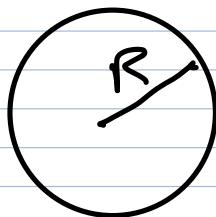
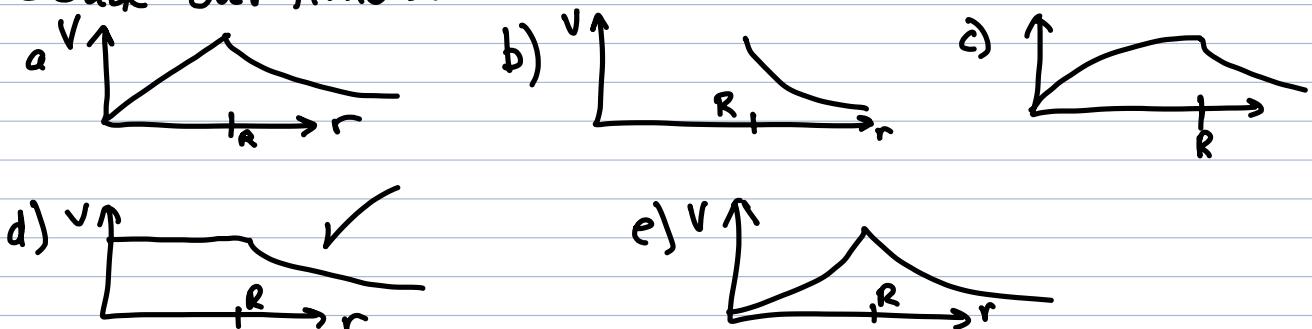
$$\underline{c < r < d} \quad V_r - V_d = \int_r^d \vec{E} \cdot d\hat{r} = -2kQ \int_r^d \frac{dr}{r^2} = \frac{2kQ}{r} \Big|_r^d = \frac{2kQ}{d} - \frac{2kQ}{r}$$

$$\Rightarrow V(r) = \frac{2kQ}{d} - \frac{2kQ}{r} + \frac{5kQ}{d}$$

Bonus fun time

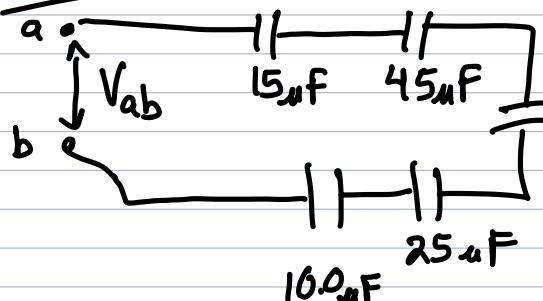


Double overtime!!



Solid conducting sphere with  
a net positive charge

Triple overtime

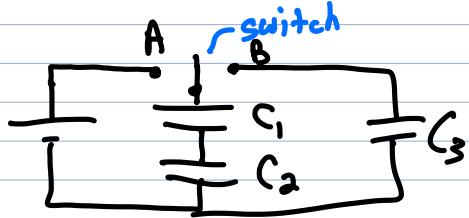


Each capacitor will explode if  $\Delta V$  across it exceeds  $30.0\text{ V}$ . .... the largest  $V_{ab}$  could be ..

The  $5\text{ }\mu\text{F}$  is most susceptible, since  $V = \frac{Q}{C} \Rightarrow$  shown: set

$V = 30V$  for  $S_{\text{on}}$ , then  $Q = 150 \mu\text{C}$

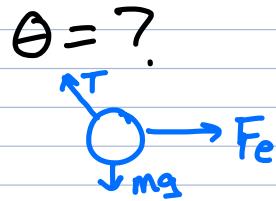
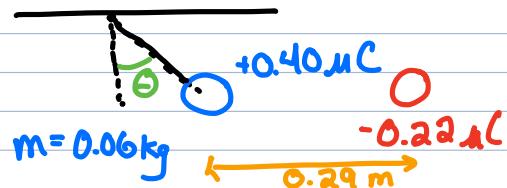
and to calculate  $V_{ab}$  use  $V_{ab} = \frac{Q}{C_{\text{eq}}} = \frac{150 \mu\text{C}}{\left(\frac{1}{10} + \frac{1}{5} + \frac{1}{45} + \frac{1}{25} + \frac{1}{15}\right)^{-1}} = 64V$



switch initially thrown to A and then to B.  
the charges are  $Q_1, Q_2, Q_3$  and

voltages  $V_1, V_2, V_3$

- a)  $V_1 = V_2 = V_3$
- b)  $V_1 + V_2 = V_3$  ←
- c)  $V_3 = 0$
- d)  $Q_1 = Q_2 = Q_3$
- e)  $Q_1 + Q_2 = Q_3$



$$\sum F_x: F_e = T \sin \theta$$

$$\sum F_y: T \cos \theta = mg \Rightarrow \cos \theta = \frac{mg}{T}$$

$$\rightarrow \sin \theta = \frac{kq_1 q_2}{T r^2}$$

$$\text{Divide these: } \tan \theta = \frac{kq_1 q_2}{r^2 mg}$$