

ch05/s4.html Concept Q

- a) Bring into contact when both are originally neutral.
i) Touch one object with charged rod ? unclear
ii) Bring charged rod near one object

b) Touch charged rod to one object. Then bring the two objects into contact

Coulomb's Law

$$F_{\text{electric}} \propto \frac{q_1 q_2}{r^2}$$

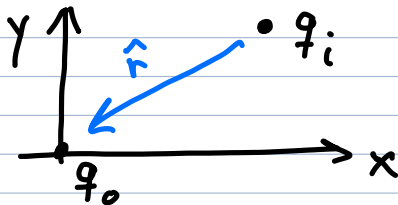
constant of proportionality $k = \frac{1}{4\pi\epsilon_0} \sim \frac{9 \cdot 10^9 \text{ Nm}^2}{\text{C}^2}$

example $+4q, +4q$ where $q = 1.60 \cdot 10^{-19} \text{ C}$ $r = 20 \text{ pm}$

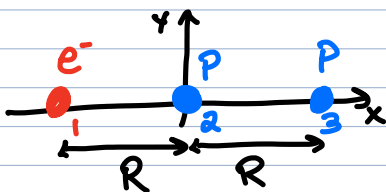
$$\Rightarrow F = 9.2 \cdot 10^{-6} \text{ N} \quad (\text{don't forget to include the factor of } 1.6 \cdot 10^{-19} \text{ twice})$$

Principle of superposition: add up all the contributions

$$\vec{F}_{\text{total on } q_0} = \sum_{i=1}^N \vec{F}_{q_i \text{ on } q_0} = \sum_{i=1}^N \frac{k q_0 q_i}{r_i^2} \hat{r}_i$$

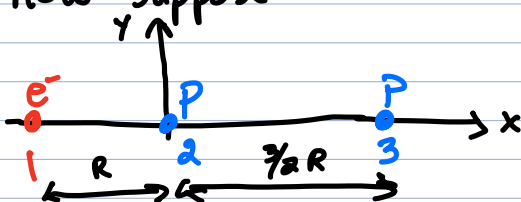


example What is the net electrostatic force on the central proton?

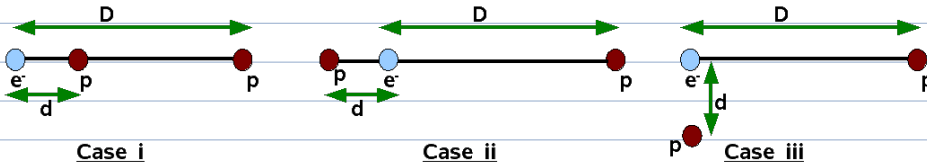


$$\begin{aligned} \vec{F}_{\text{total on 2}} &= \vec{F}_{1 \text{ on } 2} + \vec{F}_{3 \text{ on } 2} = \frac{ke^2(-\hat{i})}{R^2} + \frac{ke^2(-\hat{i})}{R^2} \\ &= \frac{-2ke^2(\hat{i})}{R^2} \end{aligned}$$

now suppose:



$$\begin{aligned} \vec{F}_{\text{total on 2}} &= \vec{F}_{1 \text{ on } 2} + \vec{F}_{3 \text{ on } 2} \\ &= \frac{ke^2(-\hat{i})}{R^2} + \frac{ke^2(-\hat{i})}{\frac{49}{4} R^2} = \frac{-13}{9} \frac{ke^2(\hat{i})}{R^2} \end{aligned}$$



Rank the arrangements according to the magnitude of the net electrostatic force on the electron due to the protons.

a) i > ii > iii

b) i > iii > ii

c) ii > i > iii

d) ii > iii > i

e) iii > i > ii

f) iii > ii > i

Case i $F_x = +\frac{k|e||-e|}{d^2} + \frac{k|e||e|}{D^2} = ke^2\left(\frac{1}{d^2} + \frac{1}{D^2}\right)$
 $F_y = 0$

Case ii $F_x = -\frac{k|e||e|}{d^2} + \frac{k|e||-e|}{D^2}$ $F_y = 0$

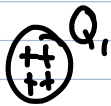
$\Rightarrow F_{net} = ke^2\left(\frac{1}{D^2} - \frac{1}{d^2}\right)$

Case iii $F_x = +\frac{k|e||-e|}{D^2}$ $F_y = -\frac{k|e||-e|}{d^2}$

$F_{net} = \sqrt{\left(\frac{ke^2}{D^2}\right)^2 + \left(\frac{-ke^2}{d^2}\right)^2} = ke^2\sqrt{\frac{1}{D^4} + \frac{1}{d^4}}$

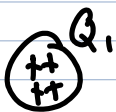
if $D=d=1$, then case i $ke^2 \cdot 2$
 case ii 0
 case iii $ke^2\sqrt{2}$ ✓

Electric Field



Point "P" in space

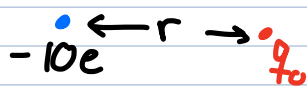
imagine placing a test charge $+q_0$ at "P"



$+q_0$

$\vec{E} = \frac{\vec{F}}{q_0}$

What is the electric field near a point charge of $-10e$?



$$\vec{F}_{\text{on } q_0} = k \frac{|q_0| |-10e|}{r^2} (-\hat{r})$$

$$\Rightarrow \vec{E} = \frac{\vec{F}}{q_0} = \frac{k |-10e| (-\hat{r})}{r^2}$$

Compare gravity to electric force. Take 2 e 's a distance r apart

$$\frac{F_e}{F_g} = \frac{k |e| |e| / r^2}{G m_e m_e / r^2} = 10^{42}$$