

Example The Lagoon Nebula has a 45 light-year diameter, it glows at 7500K, and has a density of 80 H atoms  $\frac{\text{atoms}}{\text{cm}^3}$

what is P?  $P = \frac{N}{V} k_B T = 80 \text{ cm}^{-3} \left( \frac{100 \text{ cm}}{1 \text{ m}} \right)^3 1.38 \cdot 10^{-23} \frac{\text{J}}{\text{K}} (7500 \text{ K})$

$= 8.3 \cdot 10^{12} \text{ Pa}$  or  $8.2 \cdot 10^{17} \text{ atm}$

Concept Qs SS, HTML

1)  $P = \frac{N}{V} kT$  or  $nRT$  don't know N or n [C]

2) [C]  $N = \frac{PV}{kT}$

3) [C]

4)  $K.E. = \frac{1}{2} m v_{\text{avg}}^2 = \frac{3}{2} kT$  [A]

5)  $v_{\text{avg}} = \sqrt{\frac{3kT}{m}}$  since we don't know their respective mass, we can't compare their speeds [C]

Heat capacities of gases

The K.E. of a particle is  $\frac{1}{2} m v_{\text{avg}}^2 = \frac{3}{2} kT$

→ the K.E. of a gas of N particles is  $N \frac{1}{2} m v_{\text{avg}}^2 = N \frac{3}{2} kT$

For a temperature change dT,  $dK = N \frac{3}{2} k dT = n \frac{3}{2} R dT$

We also know that  $dQ = n C_V dT$  where  $C_V$  is molar heat capacity at constant volume

so if  $dK = dQ$  then  $C_V = \frac{3}{2} R$  for an ideal gas

analogous to specific heat c for solids

Equipartition of energy

For every "degree of freedom" (of motion), a gas has energy  $\frac{1}{2} kT N$

monatomic:  $E = 3N \frac{1}{2} kT$ ,  $C_v = \frac{3}{2} R$  x, y, z

diatomic:  $E = (3+2)N \frac{1}{2} kT$ ,  $C_v = \frac{5}{2} R$  x, y, z + rotation

vibrating diatomic:  $E = (3+2+2)N \frac{1}{2} kT$ ,  $C_v = \frac{7}{2} R$  x, y, z, rotation, vibration  
the rotational and vibrational modes only kick in

for warmer gases

hot triatomic:  $E = (3+3+6)N \frac{1}{2} kT$   $C_v = \frac{12}{2} R$   
(concept Q s6.html)

i)  $C$  2 translational + 1 rotational

ii)  $E$

concept Q s9.html

$C_v = \frac{5}{2} R$  for a diatom at room temp

(see Fig 2.13 OpenStax)

$C_v = \frac{3}{2} R$  for a monatomic gas (always)

a)  $Q = nC_v \Delta T = n \frac{5}{2} R \Delta T = 1871 \text{ J}$

b)  $Q = nC_v \Delta T = n \frac{3}{2} R \Delta T = 1122 \text{ J}$

concept Q s7.html

$Q = nC_v \Delta T$  diatomic gas has higher  $C_v \Rightarrow$  requires more  $Q$  for the same  $\Delta T$

$A \Rightarrow$  energy is "wasted" on rotation

PhET simulation: states of matter

In 3 browser tabs, show Ar, Ne, O<sub>2</sub> at 50 K

Atomic #s Ar: 2.18 = 36 (actually 40 is most common isotope)

Ne: 2.10 = 20

O<sub>2</sub>: 2.28 = 32

Compare speeds; see if trend follows  $v_{avg} \propto \sqrt{\frac{T}{m}}$

$v_{avg, Ar} = \sqrt{\frac{3kT}{40 m_p}}$   $v_{avg, Ne} = \sqrt{\frac{3kT}{20 m_p}}$   $v_{avg, O_2} = \sqrt{\frac{5kT}{32 m_p}}$

$$\sqrt{\frac{3}{40}} = 0.27 \quad \sqrt{\frac{3}{20}} = 0.39 \quad \sqrt{\frac{5}{32}} = 0.39$$