

Please write directly on the exam and attach other sheets of work if necessary. Calculators are allowed. No notes or books may be used. Multiple-choice problems have only one correct answer. You may choose to circle two answers on a multiple-choice problem and, if one of them is correct, receive half credit. Circle three and if one is correct, 1/3 credit, etc. For worked problems, be complete and show all work, beginning with diagrams and fundamental, general equations used.

Kinematics  $v_{\text{avg}} = \frac{x_2 - x_1}{t_2 - t_1} = \frac{\Delta x}{\Delta t}$      $\vec{v} = \frac{d\vec{r}}{dt}$      $a_{\text{avg}} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$      $\vec{a} = \frac{d\vec{v}}{dt}$

$x_1 = x_0 + v_0 t + \frac{1}{2} a t^2$      $v_1 = v_0 + a t$      $v_1^2 = v_0^2 + 2a(x_1 - x_0)$      $a_{\text{rad}} = \frac{v^2}{R} = \frac{4\pi^2 R}{T^2}$

$\sum \vec{F} = m\vec{a}$      $\vec{w} = m\vec{g}$      $f_s \leq \mu_s N$      $f_k = \mu_k N$      $f = kv$      $f = Dv^2$      $f_{\text{spring}} = -kx$

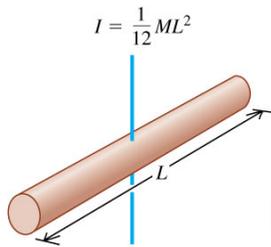
Momentum/Impulse  $\vec{p} = m\vec{v}$      $J = \Delta(mv) = F\Delta t$      $x_{\text{cm}} = \frac{\sum m_i x_i}{\sum m_i}$

Work/Energy  $W = \vec{F} \cdot \vec{s} = Fs \cos \theta$      $K_1 + U_1 + W_{\text{other}} = K_2 + U_2$      $P = \frac{\Delta W}{\Delta t} = \vec{F} \cdot \vec{v}$   
 $W = \Delta K$      $K = \frac{1}{2} mv^2$      $U_{\text{spring}} = \frac{1}{2} kx^2$      $U_{\text{grav}} = mgy$      $F = -\frac{dU}{dx}$

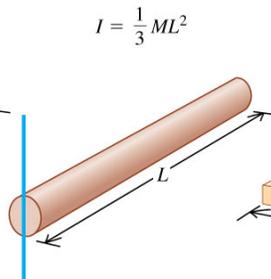
Angular Motion  $\theta_1 = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$      $\omega_1 = \omega_0 + \alpha t$      $\omega_1^2 = \omega_0^2 + 2\alpha(\theta_1 - \theta_0)$   
 $\omega = \frac{d\theta}{dt}$      $\alpha = \frac{d\omega}{dt}$      $s = r\theta$      $v = r\omega$      $a_{\text{tan}} = r\alpha$      $a_{\text{rad}} = \omega^2 r$      $2\pi = 360^\circ$

$I = \sum_i m_i r_i^2$      $I = I_{\text{cm}} + Md^2$      $\vec{\tau} = \vec{r} \times \vec{F} = rF \sin \phi$      $\sum \vec{\tau} = I\vec{\alpha}$      $W = \Delta K = \tau \Delta \theta$   
 $K_{\text{rot}} = \frac{1}{2} I \omega^2$      $K_{\text{tot}} = \frac{1}{2} mv_{\text{cm}}^2 + \frac{1}{2} I_{\text{cm}} \omega^2$      $\vec{L} = \vec{r} \times \vec{p} = rmv = I\omega$      $\Delta L = \tau \Delta t$     power =  $\tau \omega$

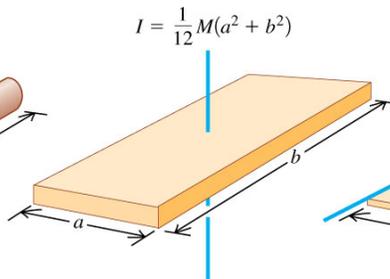
(a) Slender rod, axis through center



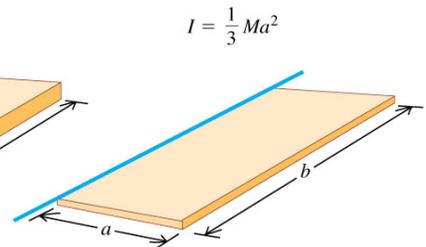
(b) Slender rod, axis through one end



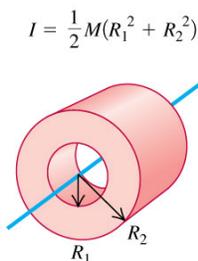
(c) Rectangular plate, axis through center



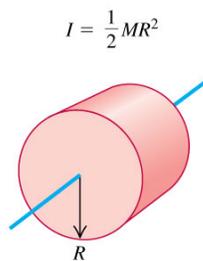
(d) Thin rectangular plate, axis along edge



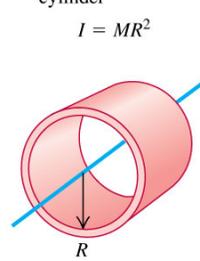
(e) Hollow cylinder



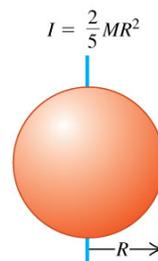
(f) Solid cylinder



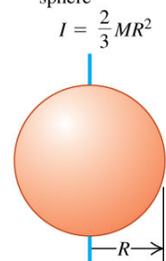
(g) Thin-walled hollow cylinder



(h) Solid sphere



(i) Thin-walled hollow sphere

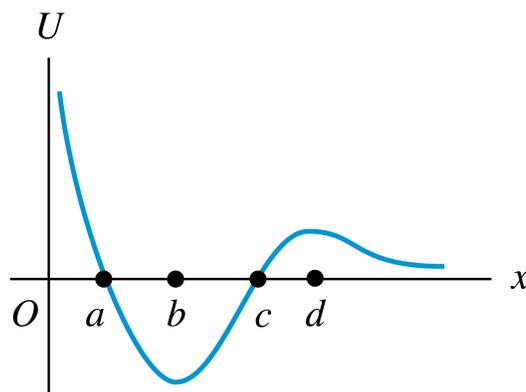




The graph at right shows the potential energy  $U$  for a particle that moves along the  $x$ -axis. Use this graph to answer questions 5 & 6.

- 5) [4 pts] The particle is initially at  $x = d$  and moves in the negative  $x$ -direction. At which of the labeled  $x$ -coordinates does the particle have the greatest *speed*?

- A) at  $x=a$
- B) at  $x=b$
- C) at  $x=c$
- D) at  $x=d$
- E) More than one of the above.



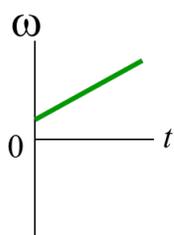
- 6) [4 pts] At which of the labeled  $x$ -coordinates is there zero force on the particle?

- A) at  $x=a$  and  $x=c$
- B) at  $x=b$  only
- C) at  $x=d$  only
- D) at  $x=b$  and  $d$
- E) misleading question – there is a force at all values of  $x$ .

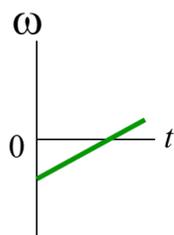
- 7) [5 pts] A car speeds up while the engine delivers constant power. Which of the following statements is correct?

- A) The car's acceleration is greater at the beginning of this process.
- B) The car's acceleration is greater at the end of this process.
- C) The car's acceleration is the same during this process.
- D) None of the above is correct.

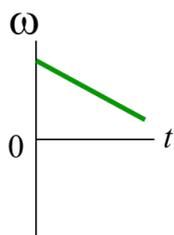
- 8) [5 pts] An object rotates with constant acceleration about an axis. The initial angular position is positive, the initial angular velocity is negative, and the angular acceleration is positive. Which of the following  $\omega$ - $t$  graphs best describes this rotational motion?



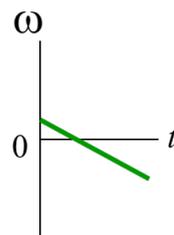
A.



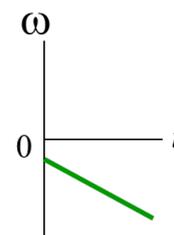
B.



C.

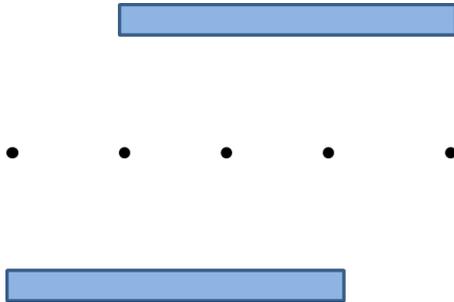


D.



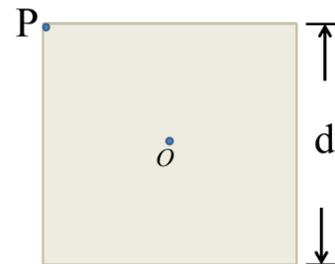
E.

- 9) [5 pts] Two geometrically identical bars with the same mass are put together according to the following figure. Circle the correct location of the center of mass of this two-bar system.



- 10) [5 pts] A square metal plate with length  $d$  on each side is pivoted about an axis through a corner (point P as indicated in the figure) and perpendicular to the plate. The mass of the plate is  $M$ , and the moment of inertia of the plate about an axis through its center of mass  $O$  and perpendicular to the plate is  $I_{CM}$ . What is the moment of inertia about the first axis through point P?

- A)  $I_p = I_{CM} + Md^2$   
 B)  $I_p = I_{CM} + M(d/2)^2$   
 C)  $I_p = I_{CM} + \frac{1}{2}Md^2$   
 D)  $I_p = \frac{1}{6}Md^2$   
 E) None of the above



- 11) [6 pts] A girl moves quickly to the center of a spinning merry-go-round, traveling along the radius of the merry-go-round. Which of the following statements are true? **Circle all that apply.**
- A) The angular speed of the system decreases.  
 B) The angular speed of the system increases.  
 C) The angular speed of the system remains constant.  
 D) The moment of inertia of the system decreases.  
 E) The moment of inertia of the system increases.  
 F) The moment of inertia of the system remains constant.  
 G) The kinetic energy of the system decreases.  
 H) The kinetic energy of the system increases.  
 I) The kinetic energy of the system remains constant.

12) [15 pts] You launch a spherical ball of mass 3.00 kg and radius 10.0 cm horizontally across a level surface, using a massless spring with spring constant  $k=500$  N/m compressed by 15.0 cm. There is no friction between the spring and the ball, so that it immediately begins rolling without slipping on the level surface. After a distance of 5 m, it begins to go up an incline with slope angle  $25^\circ$ , continuing to roll without slipping.

- A) What is the ball's center of mass velocity immediately after launch?
- B) How far does the ball travel up the incline before rolling back down?
- C) What is the angular acceleration of the ball as it rolls up the incline?

13) [15 pts] The Kuiper Belt is a population of rocky and icy bodies at Neptune's orbit and beyond. Pluto is one of the largest Kuiper Belt objects. Pluto and its largest moon, Charon, orbit each other about their center of mass. Their orbit is circular, which means that they always maintain a distance of 19,600 km from each other. Pluto has a mass of  $12.5 \times 10^{21}$  kg and Charon has a mass of  $1.62 \times 10^{21}$  kg. It takes 6.34 days for the Pluto-Charon system to complete an orbit.

- A) What is the distance between Pluto and the center of mass? Between Charon and the center of mass?
- B) What is the moment of inertia of the Pluto-Charon system?
- C) What is the total angular momentum of the Pluto-Charon system?

50.0

- 14) [15 pts] Someone fires a rifle and shoots a bullet of mass ~~5.0~~ g through an 8.00 kg pumpkin. The pumpkin is attached to a coil spring and initially rests on a frictionless, horizontal surface. The spring has a force constant of 350 N/m, and the impact compresses the spring 5.0 cm. If the speed of the bullet as it emerges from the pumpkin is 125 m/s, what is the speed of the bullet before it enters the pumpkin?