- I have three balls: small, medium, and large. I drop them all at the same time. In what order will the balls touch the ground?
- Text 'PHYSJC' and your answer to 22333

### Ch 2.5-6: Acceleration, Velocity and Position

PHYS 1210 Prof. Jang-Condell

### **Goals for Chapter 2**

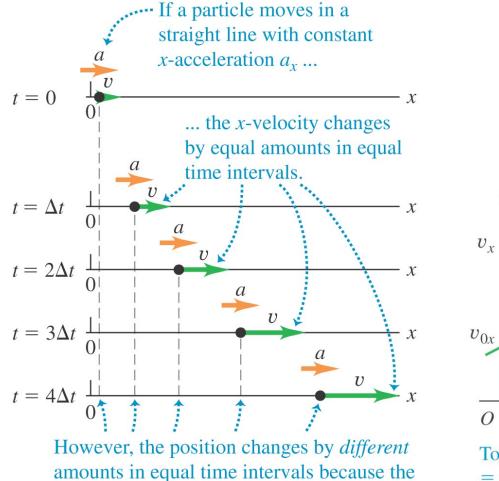
- To describe straight-line motion in terms of velocity and acceleration
- To distinguish between average and instantaneous velocity and average and instantaneous acceleration
- To interpret graphs of position versus time, velocity versus time, and acceleration versus time for straight-line motion
- To understand straight-line motion with constant acceleration
- To examine freely falling bodies
- To analyze straight-line motion when the acceleration is not constant

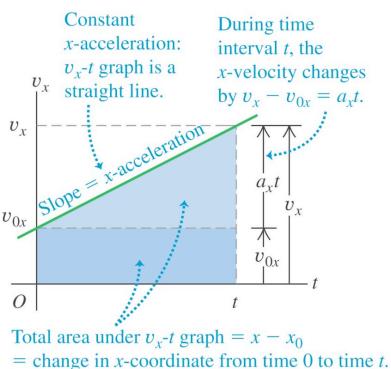
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# Constant acceleration

#### Motion with constant acceleration—Figures 2.15 and 2.17

• For a particle with constant acceleration, the velocity changes at the same rate throughout the motion.





velocity is changing.

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#### The equations of motion with constant acceleration

• The four equations shown to the below apply to any straight-line motion with constant acceleration  $a_x$ .

$$v_{x} = v_{0x} + a_{x}t$$

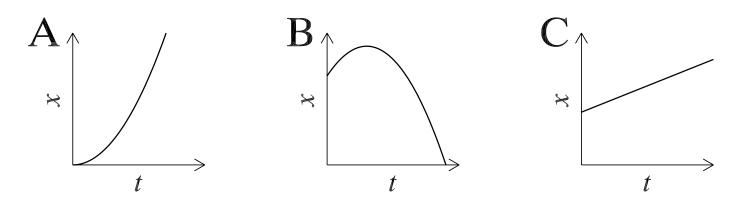
$$x = x_{0} + v_{0x}t + \frac{1}{2}a_{x}t^{2}$$

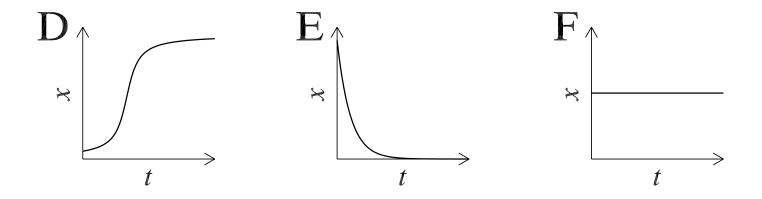
$$v_{x}^{2} = v_{0x}^{2} + 2a_{x}\left(x - x_{0}\right)$$

$$x - x_{0} = \left(\frac{v_{0x} + v_{x}}{2}\right)t$$

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### Which of these position-time plots shows constant acceleration?



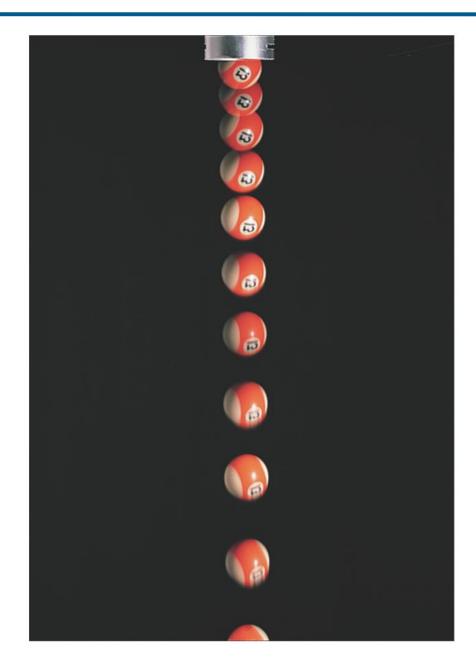


Text PHYSJC to 22333 to join the session Text your answer to 22333

### Demonstration

### **Freely falling bodies**

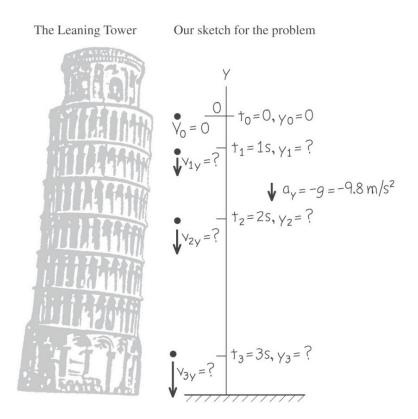
- *Free fall* is the motion of an object under the influence of only gravity.
- In the figure, a strobe light flashes with equal time intervals between flashes.
- The velocity change is the same in each time interval, so the acceleration is constant.



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### A freely falling coin

- Aristotle thought that heavy bodies fall faster than light ones, but Galileo showed that all bodies fall at the *same* rate.
- If there is no air resistance, the downward acceleration of any freely falling object is g = 9.8 m/  $s^2 = 32$  ft/s<sup>2</sup>.



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## Polleverywhere

- After I throw the ball up, at what point in the trajectory does the acceleration have the greatest magnitude?
- A. Just after leaving my hand
- B. At the highest point
- C. At the level of my hand on the way back down
- D. Just before it touches the floor
- E. None of the above

#### Is the acceleration zero at the highest point?—Figure 2.25

The vertical velocity, but *not the acceleration*, is zero at the highest point.

(a) *y*-*t* graph (curvature is (b)  $v_v$ -t graph (straight line with negative slope because  $a_v = -g$ downward because  $a_v = -g$ is negative) is constant and negative)  $v_{\rm v}$  (m/s) v(m)Before t = 1.53 s the  $\cdot \cdot$ Before t = 1.53 s 15 15 ball moves upward. the y-velocity is 10 ... After t = 1.53 s 10 positive. the ball moves 5 5 downward. 0  $\cdot t(s)$ 2 1 0 -t(s)2 4 -5After t = 1.53 s -5the y-velocity is -10negative. -10-15-15-20-20-25

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### Example Problem

You launch a water balloon vertically from the top of a tall building as shown. Neglect air resistance.

same D. Cannot tell

Text your answers to 22333

### Example Problem

You launch a water balloon vertically from the top of a tall building as shown. Neglect air resistance.

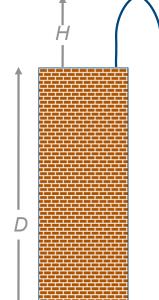
- 5. Find the initial velocity of the balloon.
- 6. Find its total time in the air.
- 7. Find its velocity when it hits the ground.

$$v_x = v_{0x} + a_x t$$

$$x = x_0 + v_{0x}t + \frac{1}{2}a_xt^2$$

$$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$$

$$x - x_0 = \left(\frac{v_{0x} + v_x}{2}\right)t$$



### **Problem-Solving Strategy**

### 1. Identify the Problem

- Picture of the problem
- Given information
- Problem to be solved
- General approach

#### 2. Set up the Physics

- Diagram axes and define variables
- Target variables
- Relevant equations

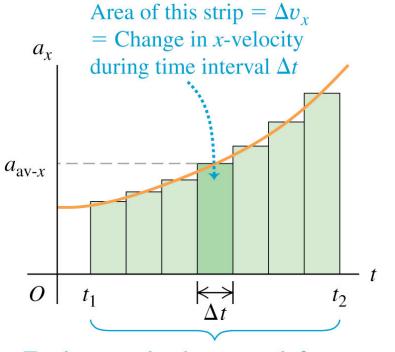
### 3. Solve the Problem

- Construct specific equations
- Outline the solution
- Solve for target variables
- 4. Evaluate your Solution
  - Units of solution correct?
  - Insert numerical values
  - Answer reasonable? Correct units?

#### **Velocity and position by integration**

- The acceleration of a car is not always constant.
- The motion may be integrated over many small time intervals to give  $v_x = v_{ox} + \int_0^t a_x dt$  and  $x = x_0 + \int_0^t v_x dt$ .





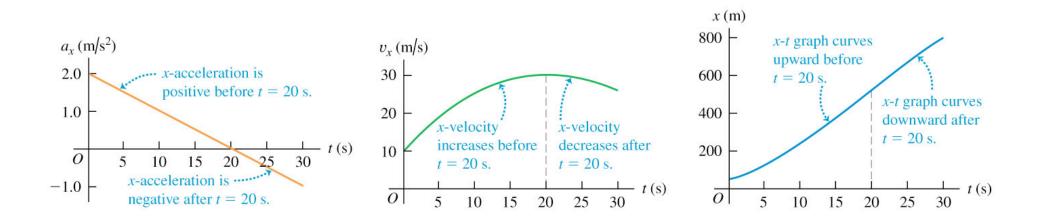
Total area under the *x*-*t* graph from  $t_1$  to  $t_2$ = Net change in *x*-velocity from  $t_1$  to  $t_2$ 

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 <u>http://www.sciencemag.org/news/</u> <u>2016/01/math-whizzes-ancient-</u> <u>babylon-figured-out-forerunner-</u> <u>calculus</u>

### Motion with changing acceleration

- Follow Example 2.9.
- Figure 2.29 illustrates the motion graphically.



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