

# Text 'PHYSJC' and your answer to 22333

You have a slingshot that fires balls at a constant initial speed. At what angle of firing will you be able to maximize the range of the slingshot? Assume any targets are the same level as the slingshot.

- A. 0-20 degrees from horizontal.
- B. 20-40 degrees
- C. 40-60 degrees
- D. 60-90 degrees
- E. None of the above

# Ch 3.4-5: Projectile Motion and Relative Velocity

PHYS 1210 - Prof. Jang-Condell

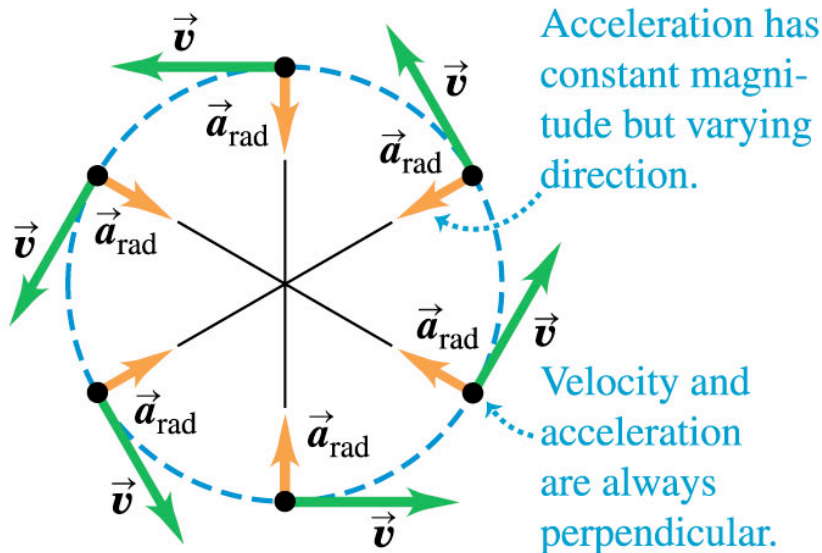
# Goals for Chapter 3

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- To use vectors to represent the position of a body
- To determine the velocity vector using the path of a body
- To investigate the acceleration vector of a body
- To describe the curved path of projectile
- To investigate circular motion
- To describe the velocity of a body as seen from different frames of reference

# Uniform Circular Motion vs. Projectile Motion

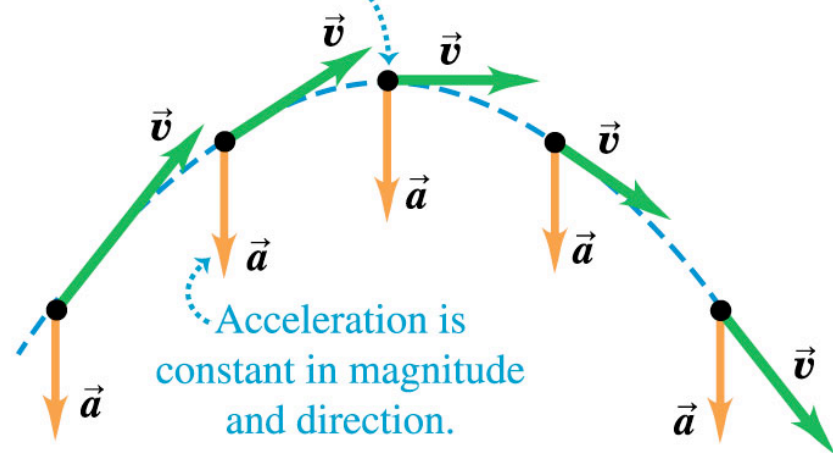
(a) Uniform circular motion



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(b) Projectile motion

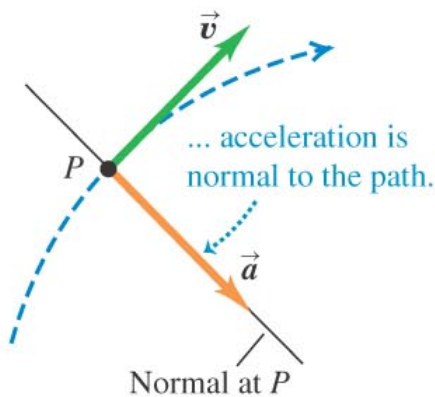
Velocity and acceleration are perpendicular only at the peak of the trajectory.



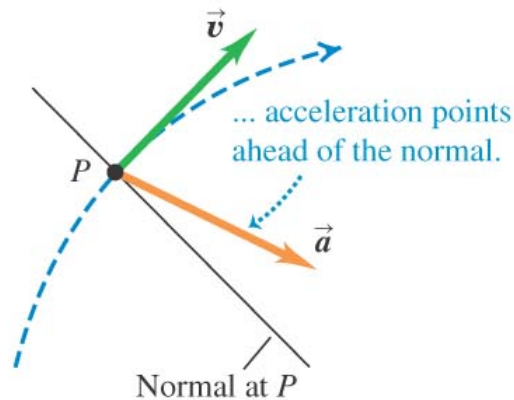
# Uniform circular motion—Figure 3.27

- For *uniform circular motion*, the speed is constant and the acceleration is perpendicular to the velocity.

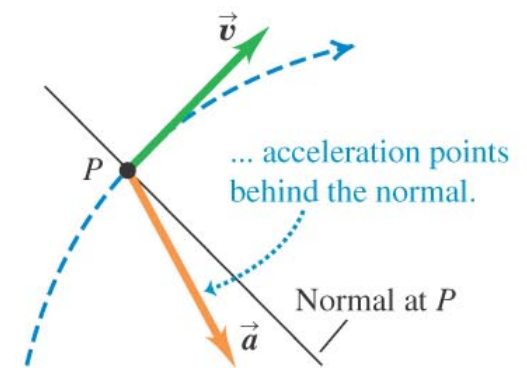
(a) When speed is constant along a curved path ...



(b) When speed is increasing along a curved path ...



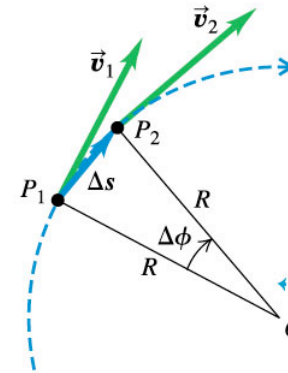
(c) When speed is decreasing along a curved path ...



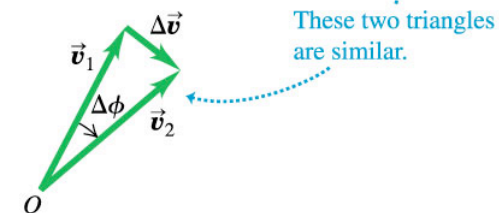
# Acceleration for uniform circular motion

- For uniform circular motion, the instantaneous acceleration always points toward the center of the circle and is called the *centripetal acceleration*.
- The magnitude of the acceleration is  $a_{\text{rad}} = v^2/R$ .
- The *period*  $T$  is the time for one revolution, and  $a_{\text{rad}} = 4\pi^2R/T^2$ .

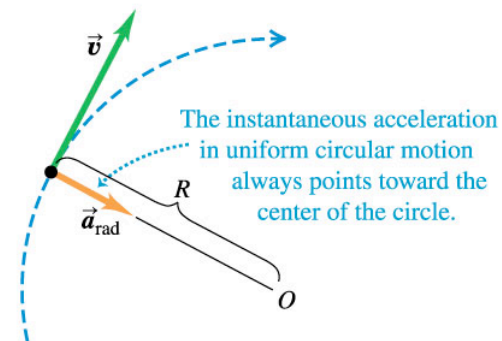
(a) A particle moves a distance  $\Delta s$  at constant speed along a circular path.



(b) The corresponding change in velocity and average acceleration

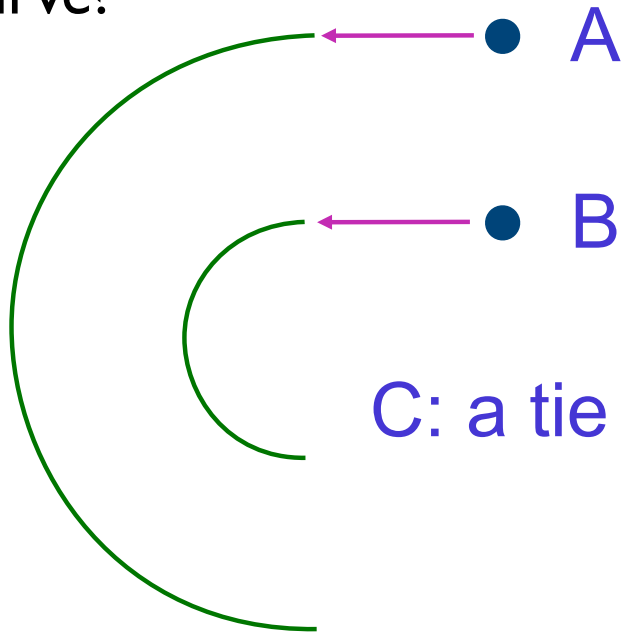


(c) The instantaneous acceleration

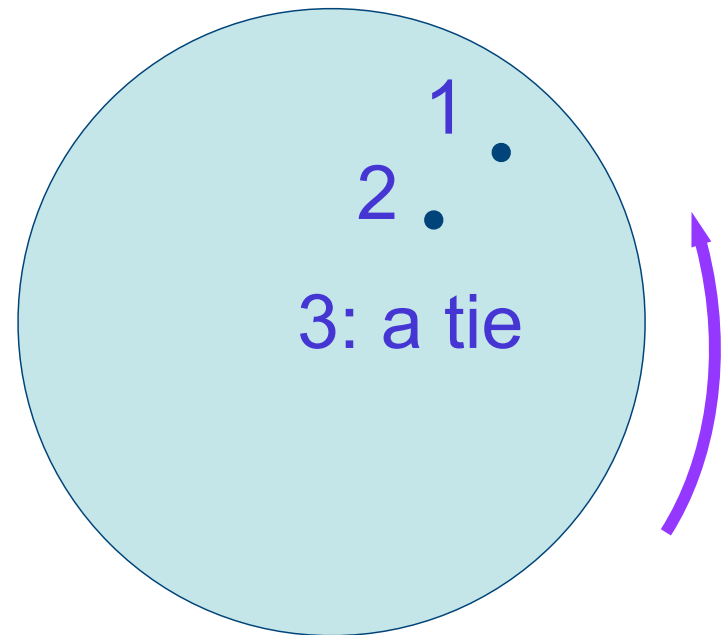


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Two balls with the **same speed** contact different semicircular guides. Which accelerates the most in the curve?



Points **1** and **2** are different distances from the center of a rotating disk. Which accelerates the most?



Enter your answer for each scenario

# Non-uniform circular motion



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Which of the following are true?



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K. The magnitude of the radial acceleration ( $a_{\text{rad}}$ ) stays constant.

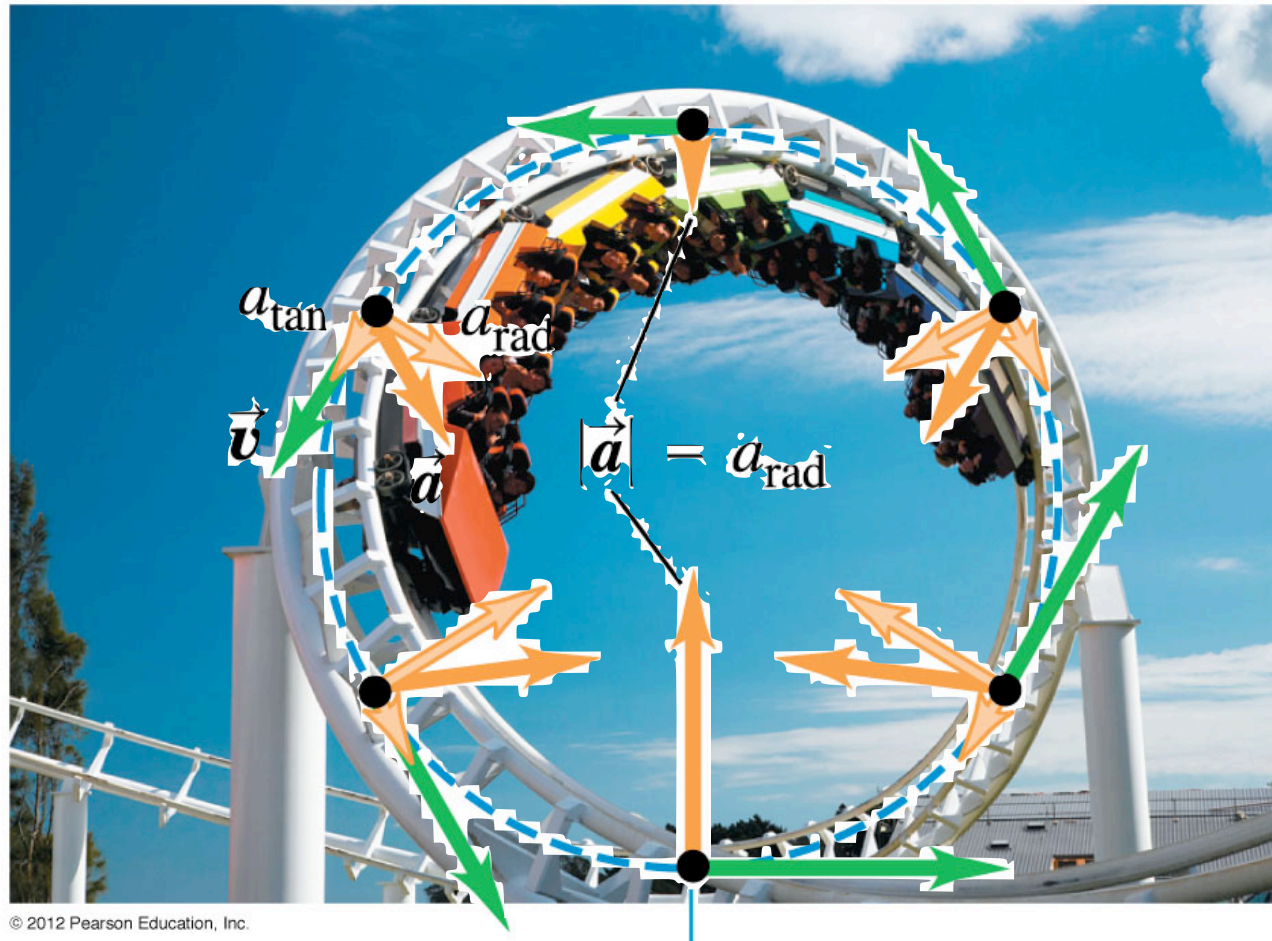
L. The magnitude of the tangential acceleration ( $a_{\text{tan}}$ ) stays constant.

M. The magnitude of the total acceleration ( $a_{\text{tot}}$ ) stays constant.

N. None of the above.

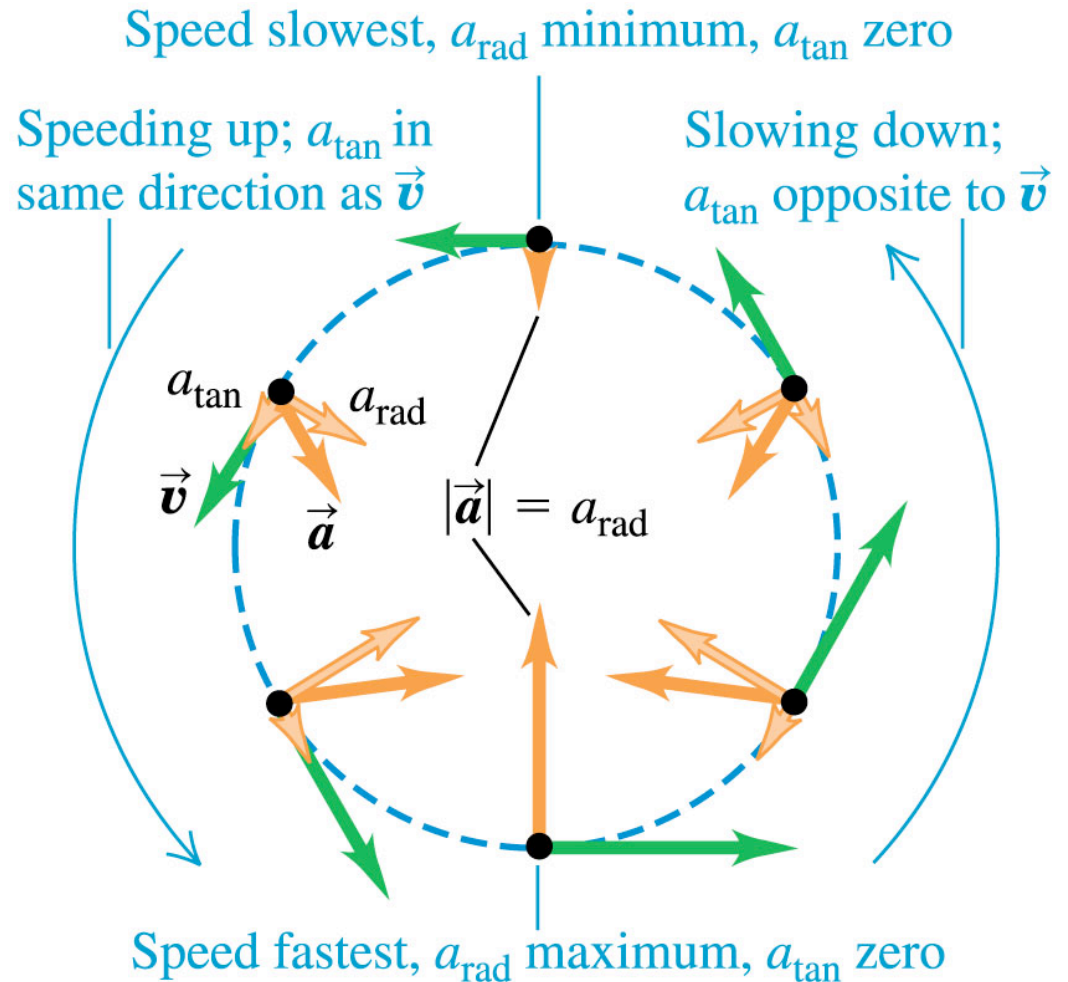
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22333

# Non-uniform circular motion



# Nonuniform circular motion—Figure 3.30

- If the speed varies, the motion is *nonuniform circular motion*.
- The radial acceleration component is still  $a_{\text{rad}} = v^2/R$ , but there is also a tangential acceleration component  $a_{\text{tan}}$  that is *parallel* to the instantaneous velocity.



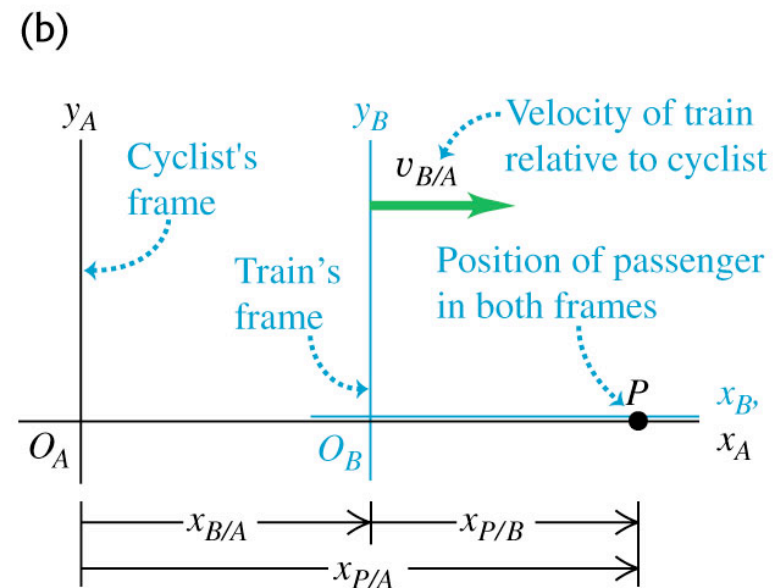
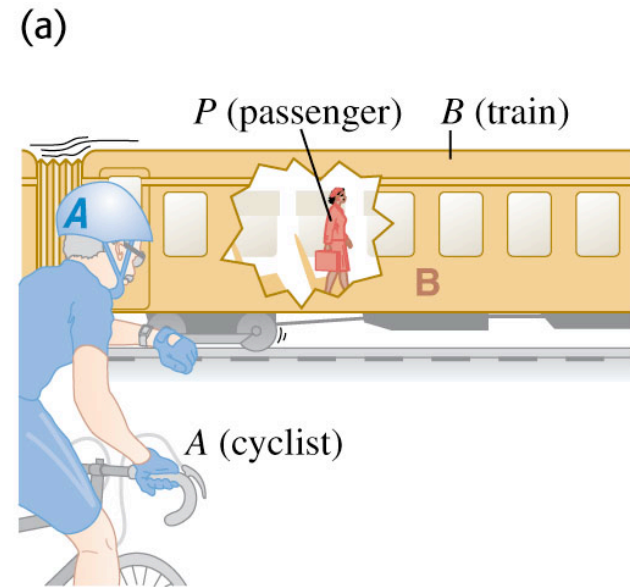
## Relative velocity—Figures 3.31 and 3.32

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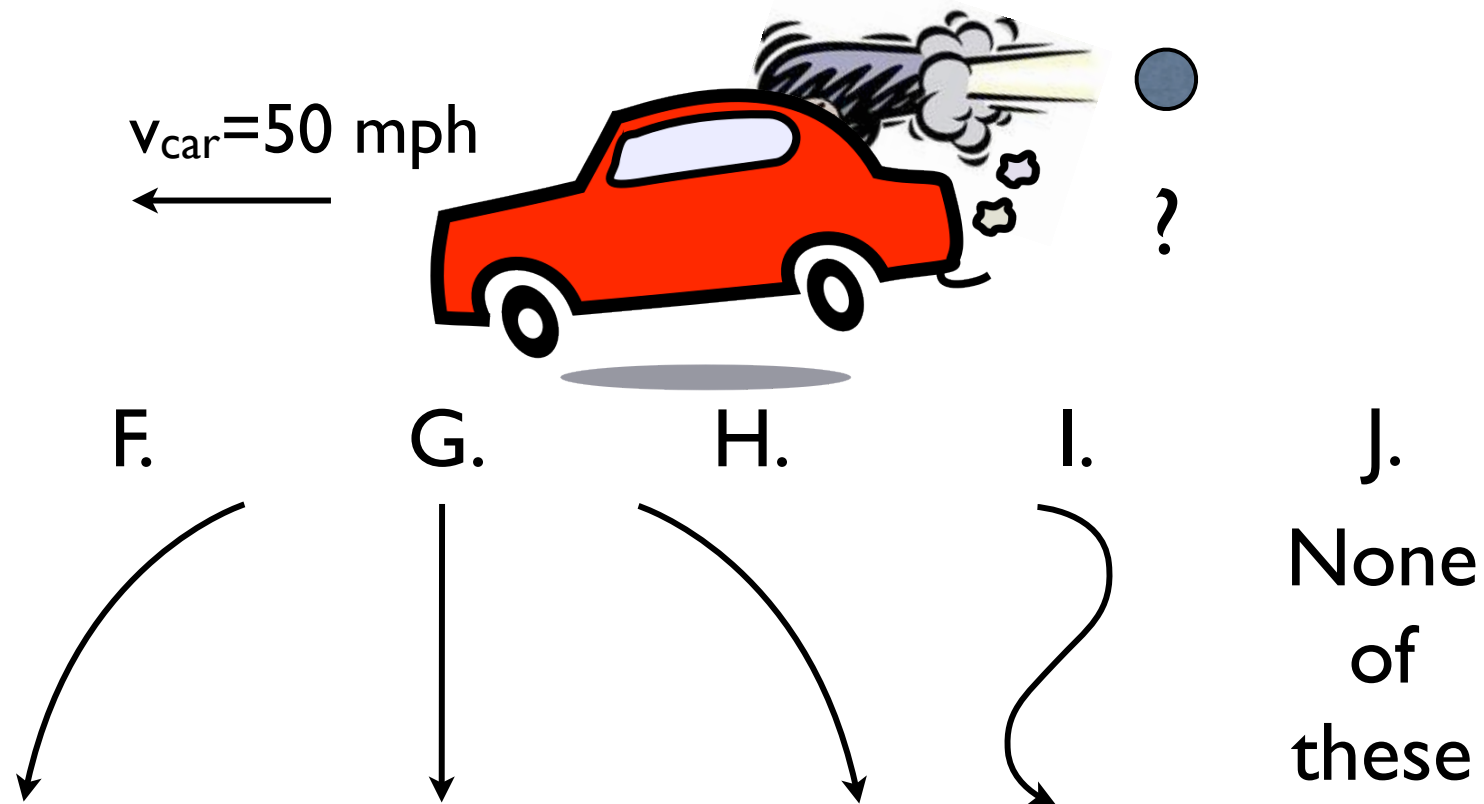
- The velocity of a moving body seen by a particular observer is called the velocity *relative* to that observer, or simply the *relative velocity*.
- A *frame of reference* is a coordinate system plus a time scale.

# Relative velocity in one dimension

- If point  $P$  is moving relative to reference frame  $A$ , we denote the velocity of  $P$  relative to frame  $A$  as  $v_{P/A}$ .
- If  $P$  is moving relative to frame  $B$  and frame  $B$  is moving relative to frame  $A$ , then the  $x$ -velocity of  $P$  relative to frame  $A$  is  $v_{P/A-x} = v_{P/B-x} + v_{B/A-x}$ .



A cannon shoots objects at an initial horizontal velocity of 50 mph. It shoots a ball out the back of car traveling 50 mph. To a stationary observer, what will the trajectory of the ball look like?



- <https://www.youtube.com/watch?v=BLuII18nhzc>

# Relative velocity in two or three dimensions

- We extend relative velocity to two or three dimensions by using vector addition to combine velocities.
- In Figure 3.34, a passenger's motion is viewed in the frame of the train and the cyclist.

