## Which of these have $\mathrm{I}=M \mathrm{R}^{2}$ ?



Text ‘PHYSJC’ and your answer to 22333

## Ch 9.5

## Moment of Inertia

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## Goals for Chapter 9

- To describe rotation in terms of angular coordinate, angular velocity, and angular acceleration
- To analyze rotation with constant angular acceleration
- To relate rotation to the linear velocity and linear acceleration of a point on a body
- To understand moment of inertia and how it relates to rotational kinetic energy
- To calculate moment of inertia


What is the speed of the block just before it hits the ground?

Two objects are at dropped from the same height at the same time. One of them is spinning as it falls, the other does not. Which object has more gravitational potential energy?
K. The spinning object.

L . The non-spinning object.
M.Both have the same potential energy.
N. Need more information

## Gravitational potential energy of an extended body

- The gravitational potential energy of an extended body is the same as if all the mass were concentrated at its center of mass.

$$
U_{\mathrm{grav}}=M g y_{\mathrm{cm}}
$$

## Diving video

## Parallel-axis Theorem

$$
I_{P}=I_{\mathrm{cm}}+M d^{2}
$$

A square metal plate with length $d$ on each side is pivoted about an axis through its center of mass (O) and perpendicular to the plate. The mass of the plate is M . What is the moment of inertia, $\mathrm{I}_{\mathrm{Cm}}$ ?


A square metal plate with length $d$ on each side is pivoted about an axis through a corner (point $P$ as indicated in the figure) and perpendicular to the plate. The mass of the plate is $M$, and the moment of inertia of the plate about an axis through its center of mass $O$ and perpendicular to the plate is Icm. What is the moment of inertia about the axis through point $P$ ?


> A. $I_{P}=I_{C M}+M d^{2}$
> B. $I_{P}=I_{C M}+M(d / 2)^{2}$
> $C . I_{P}=I_{C M}+(I / 2) M d^{2}$
> D. $I_{P}=(I / 6) M d^{2}$
> $E$. None of the above

## Moment of Inertia Calculations



$$
\begin{aligned}
& I=\int r^{2} d m \\
& d m=\rho d V \\
& I=\int \rho r^{2} d V
\end{aligned}
$$



## Simplest case: ID


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## Which of these have $\mathrm{I}=M \mathrm{R}^{2}$ ?



## Harder case: 2D

Mass element: cylindrical shell with radius $r$ and thickness $d r$


## Harder still: 3D



## Torque

## Loosen a bolt

- Which of the three equal-magnitude forces in the figure is most likely to loosen the bolt?
F. $\boldsymbol{F}_{\mathrm{a}}$
G. $F_{\mathrm{b}}$
H. $\boldsymbol{F}_{\mathrm{c}}$
I. Not enough information to decide


## Torque



When $F \perp l$, then

$$
\tau=F l
$$

## Torque

Three ways to calculate torque:


## Torque



